

Drell-Yan phenomenology in the color dipole picture revisited

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An extensive phenomenological study of the Drell-Yan (DY) process in pp collisions at various energies is performed in the color dipole framework. Besides previously studied γ^* production we have also included the Z^0 contribution relevant at large dilepton invariant masses. We investigate the DY cross section differential in invariant mass, rapidity and transverse momentum of the dilepton pair in pp collisions at RHIC and LHC. We consider three different phenomenological models for the dipole cross section and found a reasonable agreement with the available data. As a further test of the color dipole formalism, we also study the correlation function in azimuthal angle between the dilepton pair and a forward pion $\Delta\phi$ for different energies, dilepton rapidities and invariant masses. The characteristic double-peak structure of the correlation function around $\Delta\phi \simeq \pi$ found for very forward pions and low-mass dilepton pairs is sensitive to the saturation effects and can be tested by future DY measurements in pp collisions.

I. INTRODUCTION

The study of Drell-Yan (DY) processes at LHC energies provide an important test of the Standard Model (SM) as well as can supply with an additional information about New Physics beyond the SM. In particular, the DY process in $pp/pA/AA$ collisions at the LHC is an excellent tool for the investigations of strong interaction dynamics in an extended kinematical range of energies and rapidities (for a recent review see, e.g. Ref. [1]). For example, recent measurements of the gauge boson production cross section by the LHCb experiment [2] at forward rapidities have a sensitivity to x values down to 1.7×10^{-4} at the scale $Q^2 \sim M^2$ (M is the invariant mass of the dilepton) probing the parton distribution functions (PDFs) as well as soft QCD dynamics and non-linear effects in a kinematical range different from that studied by HERA.

During the last two decades several approaches have been proposed to improve the fixed-order QCD perturbation theory description of the DY process which is not reliable when two or more different hard scales are present (see e.g. Refs. [3–13]). A well-known example is the description of the transverse momentum p_T distribution of the dilepton. In the low- p_T region, $p_T \ll M$, there are two powers of $\ln(M^2/p_T^2) \gg 1$ for each additional power of the strong coupling α_s , and the DY p_T distribution calculated in fixed-order QCD perturbation theory is not reliable. Only after resummation of the large terms $\propto \alpha_s^n \ln^{2n+1}(M^2/p_T^2)$ the predictions become consistent with the data. Another example is in the case of the high energies $s \gg M^2$ when potentially large terms $\propto \alpha_s^n \ln^n(s/M^2)$ should also be resummed. In this case, the standard collinear factorisation approach should be generalized by taking into account the transverse momentum evolution of the incoming partons and QCD nonlinear effects.

One of the phenomenological approaches which effectively takes into account the higher-order QCD corrections is the color dipole formalism [14]. At high energies, color dipoles with a definite transverse separation are eigenstates of

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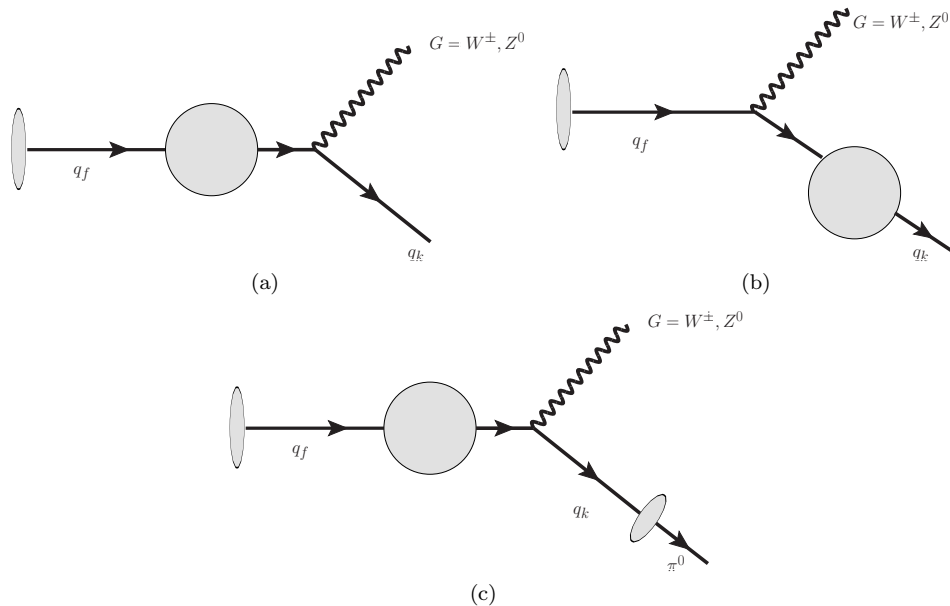


FIG. 1: Diagrams (a) and (b) represent the process of a gauge boson radiation by a quark (antiquark) of flavour f either after or before the interaction with the target color field (denoted by a shaded circle), respectively. For the considered γ, Z^0 radiation $q_k = q_f$. Diagram (c) represents the gauge boson-pion production in the color dipole picture.

interaction. The main ingredient of this formalism is the dipole-target scattering cross section which is universal and process-independent and thus can be determined phenomenologically, for example, from the Deep Inelastic Scattering (DIS) data [15]. In particular, it provides a unified description of inclusive and diffractive observables in ep scattering processes as well as other processes in hadron-hadron collisions such as DY, prompt photon, heavy quark production etc [14, 16–21]. Although cross sections are Lorentz invariant, the partonic interpretation of the corresponding processes depends on the reference frame [17]. In particular, in the framework of conventional parton model the DY process is typically considered as due to parton annihilation in the center-of-mass frame description. In the target rest frame the same process can be viewed as a bremsstrahlung of γ/Z^0 in the dipole picture as is illustrated in Figs. 1 (a) and (b). In the latter case, the radiation occurs both after and before the quark scatters off the target and the corresponding amplitudes interfere. In the high-energy limit, the projectile quark probes dense gluonic field in the target such that nonlinear effects due to multiple scatterings become important and should be taken into account.

The DY process mediated by virtual photon has been studied within the dipole framework in the literature by several authors (see e.g. Refs. [22–24]). In particular, in Ref. [23] it has been demonstrated that the dipole model provides as precise prediction for the DY cross section as the NLO collinear factorisation framework giving a solid foundation for the current more extensive study. The inclusive gauge bosons production has been previously analysed by some of the authors in Ref. [25] where predictions for the total cross sections and rapidity distributions were found to be in a good agreement with the recent LHC data. In the diffractive channel, the DY and electroweak gauge boson production processes have been studied in the dipole framework in Ref. [26].

The goal of the current work is the following. First, we update and improve previous studies. We present predictions for the transverse momentum, invariant mass and rapidity distributions for the DY pair production at RHIC and LHC energies and compare them with available data taking into account Z^0 boson contribution in addition to the virtual photon. Second, we present a detailed analysis of the azimuthal correlation between the DY pair and a forward pion (see Fig. 1(c)). Similar correlations in dihadron, real photon-hadron and dilepton-hadron channels have been previously investigated in Refs. [27–30]. In variance from the dihadron channel, the dilepton-hadron correlations can serve as an efficient probe of the initial state effects since the intermediate virtual boson (γ/Z^0) does not interact with partons inside the target hadron and therefore the final state interaction effects do not exist. In this paper, for the first time we present results for such an observable in pp collisions at RHIC ($\sqrt{s} = 200$ and 500 GeV) and LHC ($\sqrt{s} = 7$ and 14 TeV) at different M . We test three different models for the dipole cross section accounting for saturation effects [31] in order to estimate the underlined theoretical uncertainties.

This paper is organized as follows. In the next Section, we present a brief overview of gauge boson production in the color dipole framework. Moreover, we derive the differential cross section for the dilepton-hadron production in the momentum representation taking into account both virtual photon and Z^0 boson contributions. In Section III,

we present our results for the total cross sections, invariant mass, rapidity and transverse momentum distributions and compare our predictions with the available data at different energies. Predictions for future RHIC and LHC runs are also given. Furthermore, the azimuthal correlation function is evaluated for the DY-pion production in pp collisions at RHIC and LHC for different dilepton invariant masses and rapidities. For the first time, we have found a double-peak structure in the pion-dilepton correlation function around $\Delta\phi = \pi$ at forward pion rapidities. Finally, in Section IV, our main conclusions are summarized.

II. INCLUSIVE GAUGE BOSON PRODUCTION IN THE DIPOLE PICTURE

As was mentioned above, in the color dipole picture the DY process is considered as a bremsstrahlung of a virtual gauge boson G^* by a projectile quark, where $G = \gamma, Z^0, W^\pm$ [17–19] as is illustrated in Fig. 1. In the high energy limit, each of the two graphs factorizes into the production vertex for a given gauge boson times the scattering amplitude of a quark off the target. The quark scatters at different impact parameters depending on whether the gauge boson is radiated after or before the scattering. The interference between these scattering amplitudes implies that the squared matrix element for the gauge boson production is expressed in terms of the universal dipole-target cross section $\sigma_{q\bar{q}}(\rho, x)$ with transverse separation between ρ initial (q_f) and final (q_k) quark as is shown in Fig. 1.

A. Inclusive DY cross section

In order to estimate the hadronic cross section for the inclusive DY process $pp \rightarrow G^* X$ one has to note that the gauge boson carries away the light-cone momentum fraction x_1 and α from the projectile proton and quark emitting the gauge boson, respectively. Consequently, the momentum fraction of the quark is given by $x_q = x_1/\alpha$. Then the cross section for the inclusive gauge boson production with invariant mass M and transverse momentum p_T is expressed in terms of the quark (antiquark) densities q_f (\bar{q}_f) at momentum fraction x_q as follows

$$\frac{d\sigma(pp \rightarrow G^* X)}{d^2 p_T d\eta} = J(\eta, p_T) \frac{x_1}{x_1 + x_2} \sum_f \sum_{\lambda_G=L,T} \int_{x_1}^1 \frac{d\alpha}{\alpha^2} [q_f(x_1/\alpha, \mu_F^2) + \bar{q}_f(x_1/\alpha, \mu_F^2)] \frac{d\sigma_{\lambda_G}^f(qN \rightarrow qG^* X)}{d \ln \alpha d^2 p_T} \quad (1)$$

where

$$J(\eta, p_T) \equiv \frac{dx_F}{d\eta} = \frac{2}{\sqrt{s}} \sqrt{M^2 + p_T^2} \cosh(\eta) \quad (2)$$

is the Jacobian of transformation between Feynman variable $x_F = x_1 - x_2$ and pseudorapidity η of the virtual gauge boson G^* and $\mu_F^2 = p_T^2 + (1 - x_1)M^2$ is the factorization scale in quark PDFs. In practical calculations below we take $\mu_F \simeq M$, for simplicity. We have checked numerically that such a choice of the factorisation scale is a good approximation in the whole kinematical range we are concerned about in this work. The dilepton cross section analysed below is related to the inclusive $G = \gamma, Z^0$ production cross section (1) as follows

$$\frac{d\sigma(pp \rightarrow [G^* \rightarrow l\bar{l}] X)}{d^2 p_T dM^2 d\eta} = \mathcal{F}_G(M) \frac{d\sigma(pp \rightarrow G^* X)}{d^2 p_T d\eta}, \quad (3)$$

where

$$\mathcal{F}_\gamma(M) = \frac{\alpha_{em}}{3\pi M^2}, \quad \mathcal{F}_Z(M) = \text{Br}(Z^0 \rightarrow l\bar{l}) \rho_Z(M). \quad (4)$$

Here, the branching ratio $\text{Br}(Z^0 \rightarrow l\bar{l}) \simeq 0.101$, and $\rho_Z(M)$ is the invariant mass distribution of the Z^0 boson in the narrow width approximation

$$\rho_Z(M) = \frac{1}{\pi} \frac{M\Gamma_Z(M)}{(M^2 - m_Z^2)^2 + [M\Gamma_Z(M)]^2}, \quad \Gamma_Z(M)/M \ll 1, \quad (5)$$

in terms of the on-shell Z^0 boson mass, $m_Z \simeq 91.2$ GeV, and the generalized total Z^0 decay width

$$\Gamma_Z(M) = \frac{\alpha_{em} M}{6 \sin^2 2\theta_W} \left(\frac{160}{3} \sin^4 \theta_W - 40 \sin^2 \theta_W + 21 \right), \quad (6)$$

where θ_W is the Weinberg gauge boson mixing angle in the SM, $\sin^2 \theta_W \simeq 0.23$, and $\alpha_{em} = e^2/(4\pi) = 1/137$ is the fine structure constant.

The transverse momentum distribution of the gauge boson G^* can be obtained by a generalization of the well-known formulas for the photon bremsstrahlung [22, 23]. The corresponding differential cross section for a given incoming quark flavour f reads

$$\begin{aligned} \frac{d\sigma_{T,L}^f(qN \rightarrow qG^*X)}{d\ln \alpha d^2 p_T} &= \frac{1}{(2\pi)^2} \sum_{\text{quark pol.}} \int d^2 \rho_1 d^2 \rho_2 \exp[i\mathbf{p}_T \cdot (\boldsymbol{\rho}_1 - \boldsymbol{\rho}_2)] \Psi_{T,L}^{V-A}(\alpha, \boldsymbol{\rho}_1, m_f) \Psi_{T,L}^{V-A,*}(\alpha, \boldsymbol{\rho}_2, m_f) \\ &\times \frac{1}{2} [\sigma_{q\bar{q}}(\alpha \boldsymbol{\rho}_1, x_2) + \sigma_{q\bar{q}}(\alpha \boldsymbol{\rho}_2, x_2) - \sigma_{q\bar{q}}(\alpha |\boldsymbol{\rho}_1 - \boldsymbol{\rho}_2|, x_2)] , \end{aligned} \quad (7)$$

where $x_2 = x_1 - x_F$, $\boldsymbol{\rho}_1$ and $\boldsymbol{\rho}_2$ are the quark- G transverse separations in the total radiation amplitude and its conjugated counterpart, respectively. Assuming that the projectile quark is unpolarized, the products of the vector and axial-vector wave functions in Eq. (7) can be written as follows

$$\begin{aligned} \sum_{\text{quark pol.}} \Psi_{T,L}^{V-A}(\alpha, \boldsymbol{\rho}_1, m_f) \Psi_{T,L}^{V-A,*}(\alpha, \boldsymbol{\rho}_2, m_f) &= \\ = \Psi_{T,L}^V(\alpha, \boldsymbol{\rho}_1, m_f) \Psi_{T,L}^{V,*}(\alpha, \boldsymbol{\rho}_2, m_f) + \Psi_{T,L}^A(\alpha, \boldsymbol{\rho}_1, m_f) \Psi_{T,L}^{A,*}(\alpha, \boldsymbol{\rho}_2, m_f) , \end{aligned} \quad (8)$$

where the averaging over the initial and summation over final quark helicities is performed and the quark flavour dependence comes only via projectile quark mass m_f . Different components in Eq. (8) read [26]

$$\begin{aligned} \Psi_V^T \Psi_V^{T*} &= \frac{(\mathcal{C}_f^G)^2 (g_{v,f}^G)^2}{2\pi^2} \left\{ m_f^2 \alpha^4 K_0(\tau \rho_1) K_0(\tau \rho_2) + [1 + (1 - \alpha)^2] \tau^2 \frac{\boldsymbol{\rho}_1 \cdot \boldsymbol{\rho}_2}{\rho_1 \rho_2} K_1(\tau \rho_1) K_1(\tau \rho_2) \right\} , \\ \Psi_V^L \Psi_V^{L*} &= \frac{(\mathcal{C}_f^G)^2 (g_{v,f}^G)^2}{\pi^2} M^2 (1 - \alpha)^2 K_0(\tau \rho_1) K_0(\tau \rho_2) , \\ \Psi_A^T \Psi_A^{T*} &= \frac{(\mathcal{C}_f^G)^2 (g_{a,f}^G)^2}{2\pi^2} \left\{ m_f^2 \alpha^2 (2 - \alpha)^2 K_0(\tau \rho_1) K_0(\tau \rho_2) + [1 + (1 - \alpha)^2] \tau^2 \frac{\boldsymbol{\rho}_1 \cdot \boldsymbol{\rho}_2}{\rho_1 \rho_2} K_1(\tau \rho_1) K_1(\tau \rho_2) \right\} , \\ \Psi_A^L \Psi_A^{L*} &= \frac{(\mathcal{C}_f^G)^2 (g_{a,f}^G)^2}{\pi^2} \frac{\tau^2}{M^2} \left\{ \tau^2 K_0(\tau \rho_1) K_0(\tau \rho_2) + \alpha^2 m_f^2 \frac{\boldsymbol{\rho}_1 \cdot \boldsymbol{\rho}_2}{\rho_1 \rho_2} K_1(\tau \rho_1) K_1(\tau \rho_2) \right\} , \end{aligned} \quad (9)$$

where $\tau^2 = (1 - \alpha)M^2 + \alpha^2 m_f^2$, $K_{0,1}$ denote the modified Bessel functions of the second kind, and the coupling factors \mathcal{C}_f^G are defined as

$$C_f^\gamma = \sqrt{\alpha_{em}} e_f , \quad C_f^Z = \frac{\sqrt{\alpha_{em}}}{\sin 2\theta_W} , \quad C_f^{W^+} = \frac{\sqrt{\alpha_{em}}}{2\sqrt{2} \sin \theta_W} V_{f_u f_d} , \quad C_f^{W^-} = \frac{\sqrt{\alpha_{em}}}{2\sqrt{2} \sin \theta_W} V_{f_d f_u} , \quad (10)$$

with the vectorial coupling at the leading order given by

$$g_{v,f_u}^Z = \frac{1}{2} - \frac{4}{3} \sin^2 \theta_W , \quad g_{v,f_d}^Z = -\frac{1}{2} + \frac{2}{3} \sin^2 \theta_W , \quad g_{v,f}^W = 1 , \quad (11)$$

and

$$g_{a,f_u}^Z = \frac{1}{2} , \quad g_{a,f_d}^Z = -\frac{1}{2} , \quad g_{a,f}^W = 1 \quad (12)$$

in the axial-vector case. In the above formulas, $f_u = u, c, t$ and $f_d = d, s, b$ are the flavours of up- and down-type quarks, respectively, $V_{f_u f_d}$ is the CKM matrix element corresponding to $f_u \rightarrow f_d$ transition, and e_f is the charge of the projectile quark¹. In the case of projectile photon we have $g_{v,q} = 1$ and $g_{a,q} = 0$. In the present analysis, we restrict ourselves to study of dilepton $l\bar{l}$ productions channels in pp collisions and therefore we consider production of virtual γ and Z^0 bosons only. For this reason, we leave W^\pm production in the $l\bar{l}\gamma$ decay channel for future studies. Integrating over the phase space of the final quark, Eqs. (1) and (3) enable us to study the (pseudo)rapidity, transverse momentum and invariant mass distributions for the DY process.

¹ Also, we are focused only on light quark flavours $f = u, d, s$

B. Dilepton-hadron azimuthal correlations

In order to study the azimuthal angle correlation between the DY pair and a hadron in the final state, we should keep an information about the quark which radiates the virtual gauge boson G^* . This analysis can, in principle, be carried out in the impact parameter representation (for more details, see Appendix B in Ref. [22] for the γ^* case), but numerically it is rather cumbersome due to a large number of oscillating Fourier integrals. To avoid this complication we switch to the derivation of the corresponding differential cross section in momentum representation as was performed in the γ^* case in Refs. [30, 32–34]. Additionally, we extend it by incorporating Z^0 boson contribution relevant at large dilepton invariant masses. Our basic goal here is to investigate the dilepton-pion correlations accounting for both virtual γ and Z^0 contributions in pp collisions at high energies and their interference in various kinematical domains in rapidity and dilepton invariant mass. The latter can be straightforwardly generalized to the proton-nucleus case.

A generalisation of the results in Refs. [33, 34] is achieved by accounting for both vector and axial contributions in the gauge boson distribution amplitude $q \rightarrow q + G^*$ with unpolarised q and G^* . This leads to the differential cross section for the production of a virtual gauge boson G^* and a hadron h (for simplicity, we take $m_f = 0$ for $f = u, d, s$ in what follows)

$$\begin{aligned} \frac{d\sigma(pp \rightarrow hG^*X)}{dY dy_h d^2p_T d^2p_T^h} &= \int_{\frac{x_h}{1-x_1}}^1 \frac{dz_h}{z_h^2} \sum_f D_{h/f}(z_h, \mu_F^2) x_p q_f(x_p, \mu_F) (1-z) S_\perp F(x_g, k_T^g) \\ &\times \left\{ \frac{(\mathcal{C}_f^G)^2 g_{v,f}^2}{2\pi} \left[(1+(1-z)^2) \frac{z^2 k_T^{g^2}}{[P_T^2 + \epsilon_M^2][(\mathbf{P}_T + z\mathbf{k}_T^g)^2 + \epsilon_M^2]} \right. \right. \\ &\quad \left. \left. - z^2 \epsilon_M^2 \left(\frac{1}{P_T^2 + \epsilon_M^2} - \frac{1}{(\mathbf{P}_T + z\mathbf{k}_T^g)^2 + \epsilon_M^2} \right)^2 \right] \right. \\ &\quad \left. + \frac{(\mathcal{C}_f^G)^2 g_{a,f}^2}{2\pi} \left[(1+(1-z)^2) \frac{z^2 k_T^{g^2}}{[P_T^2 + \epsilon_M^2][(\mathbf{P}_T + z\mathbf{k}_T^g)^2 + \epsilon_M^2]} \right. \right. \\ &\quad \left. \left. - \frac{z^2 \epsilon_M^4}{M^2} \left(\frac{1}{P_T^2 + \epsilon_M^2} - \frac{1}{(\mathbf{P}_T + z\mathbf{k}_T^g)^2 + \epsilon_M^2} \right)^2 \right] \right\}, \end{aligned} \quad (13)$$

where the couplings \mathcal{C}_f^G and $g_{v/a,f}$ are given in Eqs. (10) – (12), $D_{h/f}$ is the fragmentation function of the projectile quark q , which has emitted the gauge boson G^* , into the produced hadron h . In addition, in Eq. (13) variables Y (\mathbf{p}_T) and y_h (\mathbf{p}_T^h) are the rapidities (transverse momenta) of the gauge boson G^* and the hadron h in the final state, respectively, z_h is the momentum fraction of the hadron h relative to the quark q it fragments from, and S_\perp is the transverse area of the target whose explicit form is not needed for our purposes here. Other kinematics variables are defined as follows

$$x_1 = \sqrt{\frac{p_T^2 + M^2}{s}} e^Y, \quad x_h \simeq \frac{p_T^h}{\sqrt{s}} e^{y_h}, \quad x_p = x_1 + \frac{x_h}{z_h}, \quad z = \frac{x_1}{x_p}, \quad \epsilon_M^2 = (1-z)M^2, \quad (14)$$

$$x_g = x_1 e^{-2Y} + \frac{x_h}{z_h} e^{-2y_h}, \quad \mathbf{k}_T^q = \frac{\mathbf{p}_T^h}{z_h}, \quad \mathbf{k}_T^g = \mathbf{p}_T + \mathbf{k}_T^q, \quad \mathbf{P}_T = (1-z)\mathbf{p}_T - z\mathbf{k}_T^q, \quad (15)$$

where x_1 and x_h are the gauge boson G and the hadron h momentum fractions taken from the incoming proton, \mathbf{P}_T is the relative transverse momentum between the gauge boson G^* and the quark q , \mathbf{k}_T^q is the transverse momentum of the quark q in the final state, \mathbf{k}_T^g is the transverse momentum of the exchanged gluon². The quantity $F(x_g, k_T^g)$ denotes the unintegrated gluon distribution function (UGDF) describing interactions of the incoming quark with the target color field, which can be obtained by a Fourier transform of the dipole cross section $\sigma_{q\bar{q}}(\rho)$ (see Ref. [29] for more details).

Integrating equation (13) over the final hadron h momentum, rapidity and relative angle between G^* and h one

² Variables z and x_p have the same physical meaning as α and $x_q \equiv x_1/\alpha$ in Eq. (1), respectively, but now they are related to the kinematic variables corresponding the final hadron z_h , y_h and p_T^h , so different notations are reserved for them to avoid confusion.

arrives at the inclusive gauge boson production cross section

$$\begin{aligned}
\frac{d\sigma(pp \rightarrow G^* X)}{dY d^2 p_T} &= \int_{x_1}^1 \frac{dz}{z} \int d^2 k_T^g \sum_f x_p q_f(x_p, \mu_F) S_\perp F(x_g, k_T^g) \\
&\times \left\{ \frac{(\mathcal{C}_f^G)^2 g_{v,f}^2}{2\pi} \left[(1 + (1-z)^2) \frac{z^2 k_T^{g^2}}{[p_T^2 + \epsilon_M^2] [(\mathbf{p}_T - z\mathbf{k}_T^g)^2 + \epsilon_M^2]} \right. \right. \\
&\quad \left. \left. - z^2 \epsilon_M^2 \left(\frac{1}{p_T^2 + \epsilon_M^2} - \frac{1}{(\mathbf{p}_T - z\mathbf{k}_T^g)^2 + \epsilon_M^2} \right)^2 \right] \right. \\
&\quad \left. + \frac{(\mathcal{C}_f^G)^2 g_{a,f}^2}{2\pi} \left[(1 + (1-z)^2) \frac{z^2 k_T^{g^2}}{[p_T^2 + \epsilon_M^2] [(\mathbf{p}_T - z\mathbf{k}_T^g)^2 + \epsilon_M^2]} \right. \right. \\
&\quad \left. \left. - \frac{z^2 \epsilon_M^4}{M^2} \left(\frac{1}{p_T^2 + \epsilon_M^2} - \frac{1}{(\mathbf{p}_T - z\mathbf{k}_T^g)^2 + \epsilon_M^2} \right)^2 \right] \right\}. \tag{16}
\end{aligned}$$

Eqs. (13) and (16) allow us to construct the correlation function $C(\Delta\phi)$, which depends on the azimuthal angle difference $\Delta\phi$ between the trigger and associate particles. Experimentally, this coincidence probability is defined in terms of the yield of the correlated trigger and associated particle pairs $N_{pair}(\Delta\phi)$ and the trigger particle yield N_{trig} as the following ratio: $C(\Delta\phi) = N_{pair}(\Delta\phi)/N_{trig}$. Therefore, azimuthal correlations are investigated through a coincidence probability defined in terms of a trigger particle, which could be either the gauge boson or the hadron. Here we assume the former as trigger particle, so that the correlation function is written as

$$C(\Delta\phi) = \frac{2\pi \int_{p_T, p_T^h > p_T^{\text{cut}}} dp_T p_T \frac{d\sigma(pp \rightarrow h G^* X)}{dY dy_h d^2 p_T d^2 p_T^h}}{\int_{p_T > p_T^{\text{cut}}} dp_T p_T \frac{d\sigma(pp \rightarrow G^* X)}{dY d^2 p_T}}, \tag{17}$$

where p_T^{cut} is the experimental low cut-off on transverse momenta of the resolved G^* (or dilepton) and h , $\Delta\phi$ is the angle between them.

C. Dipole cross section

The main ingredient of the dipole model is the dipole cross section $\sigma_{q\bar{q}}(\rho, x)$, which represents elastic scattering of a $q\bar{q}$ dipole of transverse separation ρ at Bjorken x off a nucleon [35]. It is known to vanish quadratically $\sigma_{q\bar{q}}(\rho, x) \propto \rho^2$ as $\rho \rightarrow 0$ due to color screening which is the color transparency property [35–37]. It cannot be predicted reliably from the first principles because of poorly known higher-order perturbative QCD corrections and non-perturbative effects. In particular, it should contain an information about non-linear QCD effects in the hadronic wave function (see e.g. Ref. [31]). In recent years several groups have constructed a number of viable phenomenological models based on saturation physics and fits to the HERA and RHIC data (see e.g. Refs. [15, 38–49]).

Since our goal is to extend previous DY studies to the kinematical range probed by the massive gauge boson production, where the main contribution comes from the small dipoles, in what follows we will consider two distinct phenomenological models which take into account the DGLAP evolution as well as the saturation effects. The first one is the model proposed in Ref. [45], denoted BGBK hereafter, where the dipole cross section is given by

$$\sigma_{q\bar{q}}(\rho, x) = \sigma_0 \left[1 - \exp \left(- \frac{\pi^2}{\sigma_0 N_c} \rho^2 \alpha_s(\mu^2) x g(x, \mu^2) \right) \right], \tag{18}$$

where $N_c = 3$ is the number of colors, $\alpha_s(\mu^2)$ is the strong coupling constant at the scale μ^2 which is related to the dipole size ρ as $\mu^2 = C/\rho^2 + \mu_0^2$, with C , μ_0 and σ_0 parameters fitted to HERA data. Moreover, in this model, the gluon density evolves according to DGLAP equation [51] accounting for gluons only

$$\frac{\partial x g(x, \mu^2)}{\partial \ln \mu^2} = \frac{\alpha_s(\mu^2)}{2\pi} \int_x^1 dz P_{gg}(z) \frac{x}{z} g\left(\frac{x}{z}, \mu^2\right), \tag{19}$$

where the gluon density at initial scale μ_0^2 is parametrized as

$$x g(x, \mu_0^2) = A_g x^{-\lambda_g} (1-x)^{5.6}. \tag{20}$$

The best fit values of the model parameters are the following: $A_g = 1.2$, $\lambda_g = 0.28$, $\mu_0^2 = 0.52 \text{ GeV}^2$, $C = 0.26$ and $\sigma_0 = 23 \text{ mb}$. This model was generalized in Ref. [47] in order to take into account the impact parameter dependence of the dipole cross section and to describe exclusive observables at HERA. In this model, denoted as IP-SAT hereafter, the corresponding dipole cross section is given by

$$\sigma_{q\bar{q}}(\rho, x) = 2 \int d^2b \left[1 - \exp \left(-\frac{\pi^2}{2N_c} \rho^2 \alpha_s(\mu^2) x g(x, \mu^2) T_G(\mathbf{b}) \right) \right] \quad (21)$$

with the evolution of the gluon distribution given by Eq. (19). The Gaussian impact parameter dependence is given by $T_G(\mathbf{b}) = (1/2\pi B_G) \exp(-b^2/2B_G)$, where B_G is a free parameter extracted from the t -dependence of the exclusive ep data. The parameters of this model were updated in Ref. [48] by fitting to the recent high precision HERA data [50] providing the following values: $A_g = 2.373$, $\lambda_g = 0.052$, $\mu_0^2 = 1.428 \text{ GeV}^2$, $B_G = 4.0 \text{ GeV}^2$ and $C = 4.0$.

\sqrt{s} (TeV)	GBW	BGBK	IP-SAT	DATA (nb)
7	0.950	1.208	0.986	0.937 ± 0.037 (ATLAS) 0.974 ± 0.044 (CMS)
8	1.083	1.427	1.183	1.15 ± 0.37 (CMS)
14	1.852	2.797	2.514	–

TABLE I: Comparison between the GBW, BGBK and IP-SAT predictions for the total cross sections for Z^0 boson production at different values of the c.m. energy. The experimental results are from Refs. [52–54]. The cross sections are given in nanobarns.

Finally, for comparison with previous results available in the literature, we also consider the Golec-Biernat–Wusthoff (GBW) model [15] based upon a simplified saturated form

$$\sigma_{q\bar{q}}(\rho, x) = \sigma_0 \left(1 - e^{-\frac{\rho^2 Q_s^2(x)}{4}} \right) \quad (22)$$

with the saturation scale

$$Q_s^2(x) = Q_0^2 \left(\frac{x_0}{x} \right)^\lambda, \quad (23)$$

where the model parameters $Q_0^2 = 1 \text{ GeV}^2$, $x_0 = 3.04 \times 10^{-4}$ (4.01×10^{-5}), $\lambda = 0.288$ (0.277) and $\sigma_0 = 23.03$ (29) mb were obtained from the fit to the DIS data without (with) the contribution of the charm quark, respectively.

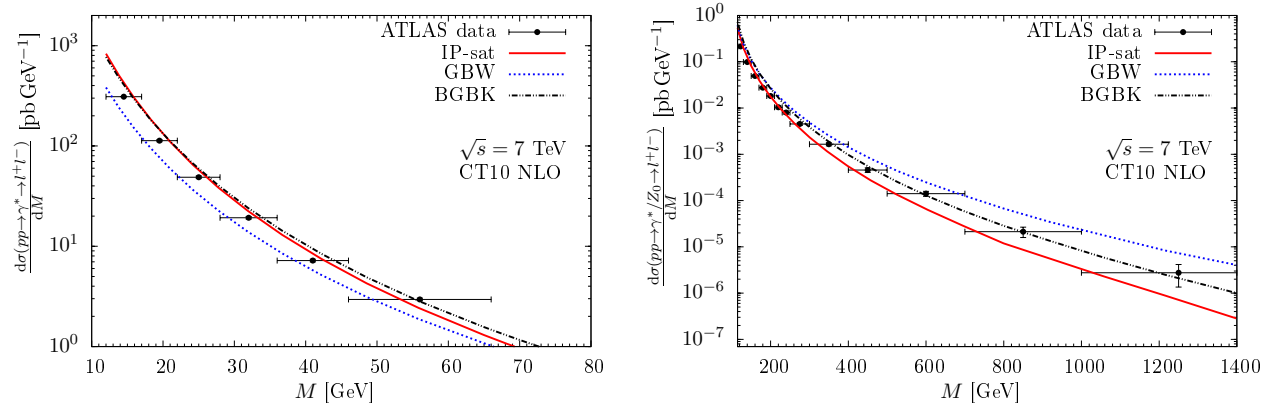


FIG. 2: The DY pair invariant mass distribution of the process $pp \rightarrow \gamma^*/Z^0 \rightarrow l\bar{l}$ at $\sqrt{s} = 7 \text{ TeV}$ in low (left panel) and high (right panel) invariant mass ranges compared to the data from the ATLAS Collaboration [55, 56] for three different parametrisations of the dipole cross section.

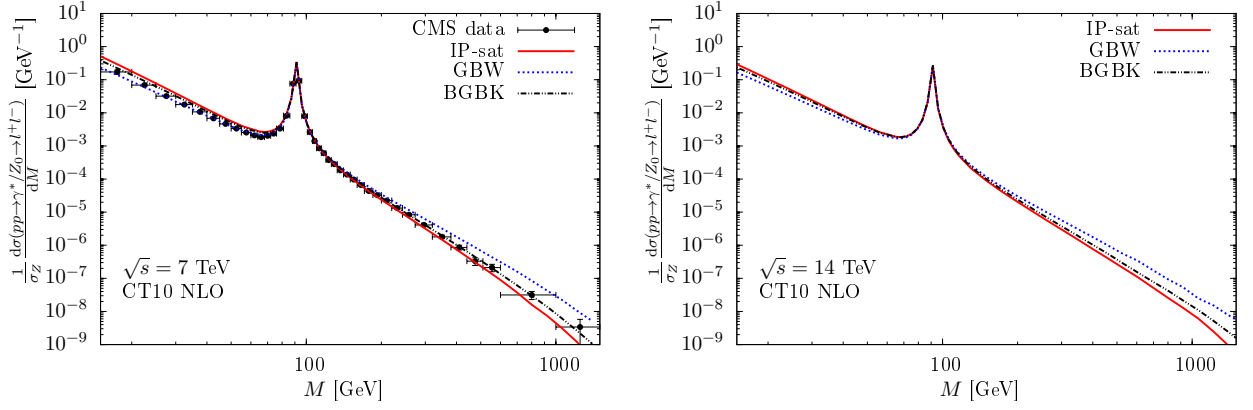


FIG. 3: The DY pair invariant mass distribution of the process $pp \rightarrow \gamma^*/Z^0 \rightarrow \ell\bar{\ell}$ at $\sqrt{s} = 7$ TeV compared to the data from the CMS collaboration [57] for three different parametrisations of the dipole cross section in the left panel. The corresponding predictions are shown for $\sqrt{s} = 14$ TeV in the right panel.

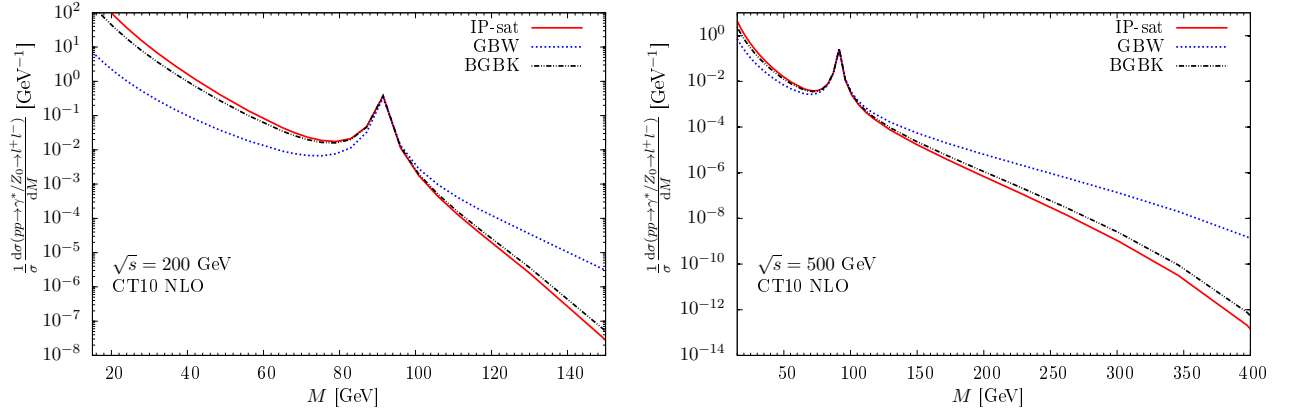


FIG. 4: The DY pair invariant mass distribution of the process $pp \rightarrow \gamma^*/Z^0 \rightarrow \ell\bar{\ell}$ at RHIC Run I ($\sqrt{s} = 200$ GeV) and II ($\sqrt{s} = 500$ GeV) energies for three different parametrisations of the dipole cross section.

III. NUMERICAL RESULTS

In what follows, we present our predictions for the DY pair production in the process $pp \rightarrow \gamma^*/Z^0 \rightarrow \ell\bar{\ell}$ obtained by using the color dipole formalism and the three phenomenological models for the dipole cross section discussed in the previous Section. Following Ref. [15], in calculations of the DY pair production cross sections we take the quark mass values to be $m_u = m_d = m_s = 0.14$ GeV, $m_c = 1.4$ GeV and $m_b = 4.5$ GeV, and employ the CT10 NLO parametrization for the projectile quark PDFs [62] with the factorization scale $\mu_F = M$.

A. Predictions for DY pair production cross sections

To start with, in Table I we present our results for the total Z^0 production cross sections for several parameterisations of the dipole cross section and different c.m. energies accessible at the LHC. The GBW model gives the cross section value at $\sqrt{s} = 7$ TeV smaller than that obtained by using the IP-SAT model which correctly treats the region of large transverse momenta due to DGLAP evolution (small dipoles). The DY cross section obtained by using the BGBK model turns out to be somewhat higher than the 7 TeV data while the GBW and IP-SAT are well within the error bars while all three models describe $\sqrt{s} = 8$ TeV data rather well. It is worth to mention that in comparison to Ref. [25] we obtain somewhat larger Z^0 cross sections for the GBW case due to an extra factor $x_1/(x_1 + x_2)$ and the use of the NLO quark PDFs.

Such a fairly good description of the LHC data on the total Z^0 cross section naturally motivates a more detailed

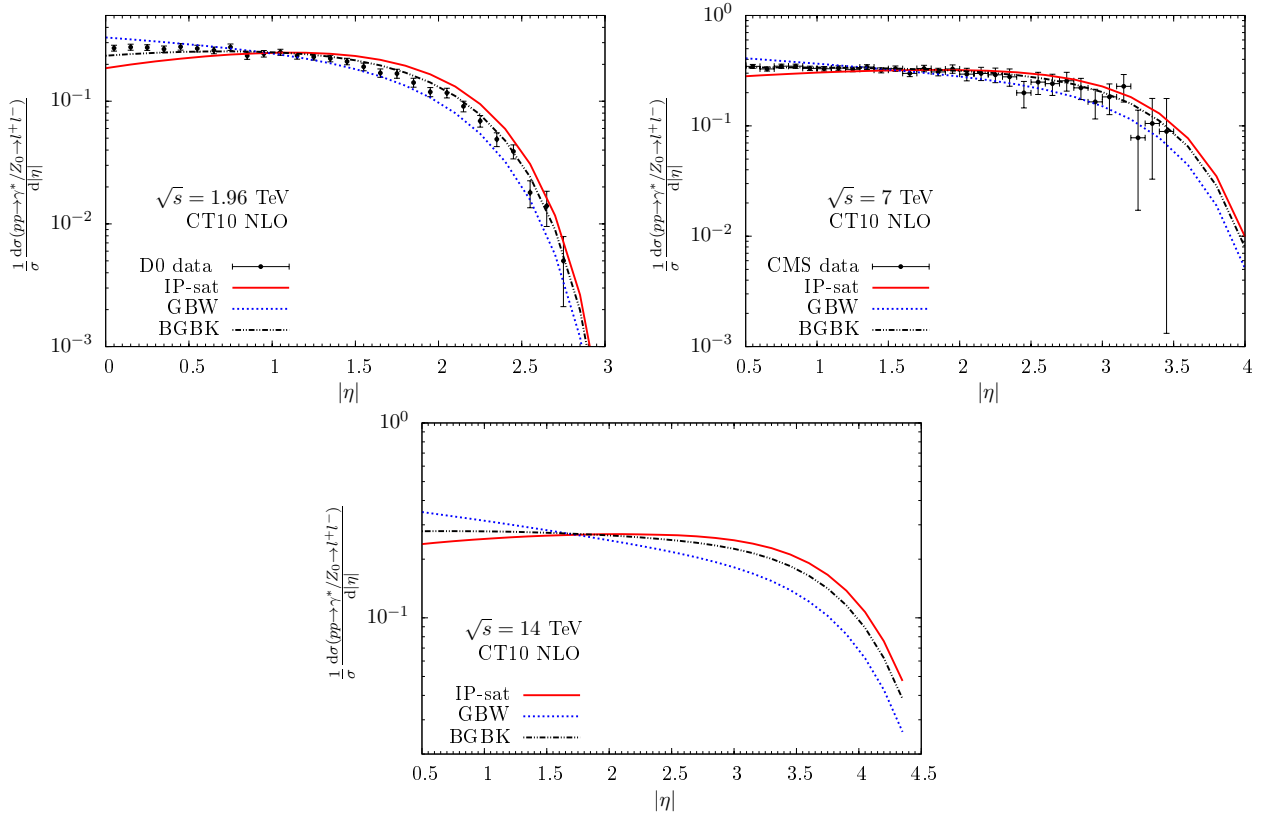


FIG. 5: The Z^0 boson rapidity distribution for different center of mass energies: $\sqrt{s} = 1.96$ TeV (top left panel), 7 TeV (top right panel) and 14 TeV (bottom panel) versus data from the D0 [58] and CMS [59] Collaborations.

analysis of the DY cross section differential in dilepton invariant mass, rapidity and transverse momentum. In Fig. 2 we compare our predictions for the invariant mass distributions with the recent ATLAS data in low and high M ranges. We conclude that the dipole cross section parameterisations including the DGLAP evolution via the gluon PDF describe the DY data better compared to the GBW model, especially at high invariant masses. The large invariant mass region prefers a fairly large Z^0 contribution as well as its interference with γ^* in the considered dilepton channel. This is clearly seen in the left panel of Fig. 3 where we present a comparison of the CMS data with predictions using three different parameterisations of the dipole cross section. Indeed, the DGLAP evolution, included in both IP-SAT and BGBK models leads to a better agreement with the data at large M in comparison with the GBW model. Our predictions for pp collisions at $\sqrt{s} = 14$ TeV are presented in the right panel of Fig. 3. Considering that similar measurements can be performed at RHIC, in Fig. 4 we show our results for the dilepton invariant mass distributions corresponding to the c.m. energies of Run I ($\sqrt{s} = 200$ GeV) and II ($\sqrt{s} = 500$ GeV). While the M -distributions corresponding to the IP-SAT and BGBK models are rather close to each other, the GBW predictions significantly differ from them away from the Z^0 peak, in both low and, especially, high invariant mass ranges.

In Fig. 5 we present our predictions for the Z^0 boson rapidity distribution at different c.m. energies corresponding to Tevatron $\sqrt{s} = 1.96$ TeV (top left panel) and LHC Run I $\sqrt{s} = 7$ TeV (top right panel). These results show that the IP-SAT and GBW models deviate from data in the central rapidity region while the BGBK predictions come closer to the data in the whole rapidity range. It is worth to emphasize that specifically for the Tevatron energy and for central rapidities, the results are rather sensitive to the behaviour of the dipole cross section at large values of x , which is not under control in the considered formalism. At larger rapidities we obtain a reasonable description of the data though. The future LHC data at $\sqrt{s} = 14$ TeV at large $M > m_Z$ can be used to put even stronger constraints on the dipole model parameterisations (see the bottom panel in Fig. 5) whose predictions significantly differ in the large rapidity region.

We turn now to a discussion of the transverse momentum distributions of the DY pair production cross section. In what follows, we take into account that heavy gauge boson and highly virtual photon production implies that typical dipole separations are small, i.e. $\rho \sim 1/\tau \ll 1/Q_s(x_2)$ ($\alpha \ll 1$). In this case, we can take the quadratic form of the

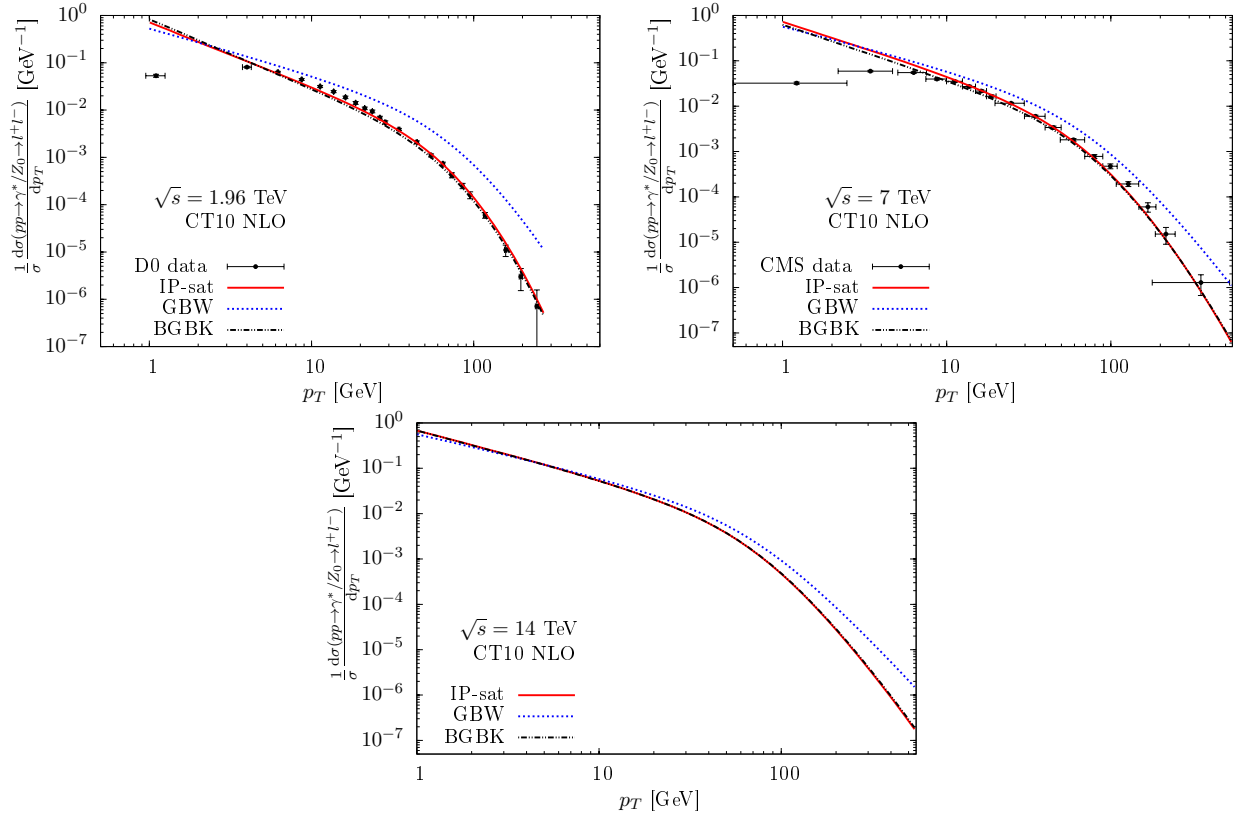


FIG. 6: The transverse momentum distributions of Z^0 bosons in pp collisions at $\sqrt{s} = 1.96$ TeV (top left panel), 7 TeV (top right panel) and 14 TeV (bottom panel) versus data from the D0 [61] and CMS [59] Collaborations.

dipole cross section as follows

$$\sigma(\rho, x) \approx \omega(x)\rho^2, \quad \omega(x) = \frac{\pi^2}{2N_c} \alpha_s(\mu^2) xg(x, \mu^2) T_G(\mathbf{b}), \quad (24)$$

for the IP-SAT model (a similar analysis can be done for the GBW and BGBK models), such that the Fourier integral in Eq. (7) can be performed analytically. Then the square bracket in Eq. (7) can be written as

$$\sigma_{q\bar{q}}(\alpha\boldsymbol{\rho}_1, x) + \sigma_{q\bar{q}}(\alpha\boldsymbol{\rho}_2, x) - \sigma_{q\bar{q}}(\alpha|\boldsymbol{\rho}_1 - \boldsymbol{\rho}_2|, x) \approx \alpha^2(\boldsymbol{\rho}_1 \cdot \boldsymbol{\rho}_2)\omega(x). \quad (25)$$

The ρ -dependent parts of the gauge boson wave functions in Eq. (9) lead to the following two Fourier integrals in the DY cross section (for more details, see Appendix B in Ref. [22])

$$J_1(p_T, \tau) = \int d^2\rho_1 d^2\rho_2 (\boldsymbol{\rho}_1 \cdot \boldsymbol{\rho}_2) K_0(\tau\rho_1) K_0(\tau\rho_2) \exp[i\mathbf{p}_T \cdot (\boldsymbol{\rho}_1 - \boldsymbol{\rho}_2)] = 16\pi^2 \frac{p_T^2}{(\tau^2 + p_T^2)^4} \quad (26)$$

$$J_2(p_T, \tau) = \int d^2\rho_1 d^2\rho_2 \frac{(\boldsymbol{\rho}_1 \cdot \boldsymbol{\rho}_2)^2}{\rho_1\rho_2} K_1(\tau\rho_1) K_1(\tau\rho_2) \exp[i\mathbf{p}_T \cdot (\boldsymbol{\rho}_1 - \boldsymbol{\rho}_2)] = 8\pi^2 \frac{\tau^4 + p_T^4}{\tau^2(\tau^2 + p_T^2)^4}. \quad (27)$$

The considered small dipole limit is valid as long as the hard scale $\tau \sim \mu_F \sim M$ is large enough compared to the saturation scale Q_s . One should note, at low transverse momenta (e.g. $p_T \lesssim 3 - 5$ GeV at the LHC) the contribution of an intrinsic primordial transverse momentum of the projectile quark in the incoming proton wave function and the corresponding Sudakov suppression can be important [60]. We postpone the analysis of these effects within the dipole formalism for a future investigation.

We present our predictions for the dilepton p_T distribution in Fig. 6 for pp collisions at various c.m. energies: $\sqrt{s} = 1.96$ TeV (top left panel), 7 TeV (top right panel) and 14 TeV (bottom panel). As was anticipated above, these predictions do not describe the experimental data in the low p_T region. On the other hand, at large $p_T > 5$ GeV the data are well described by the DGLAP-evolved dipole models IP-SAT and BGBK, but not GBW. In Fig. 7 we

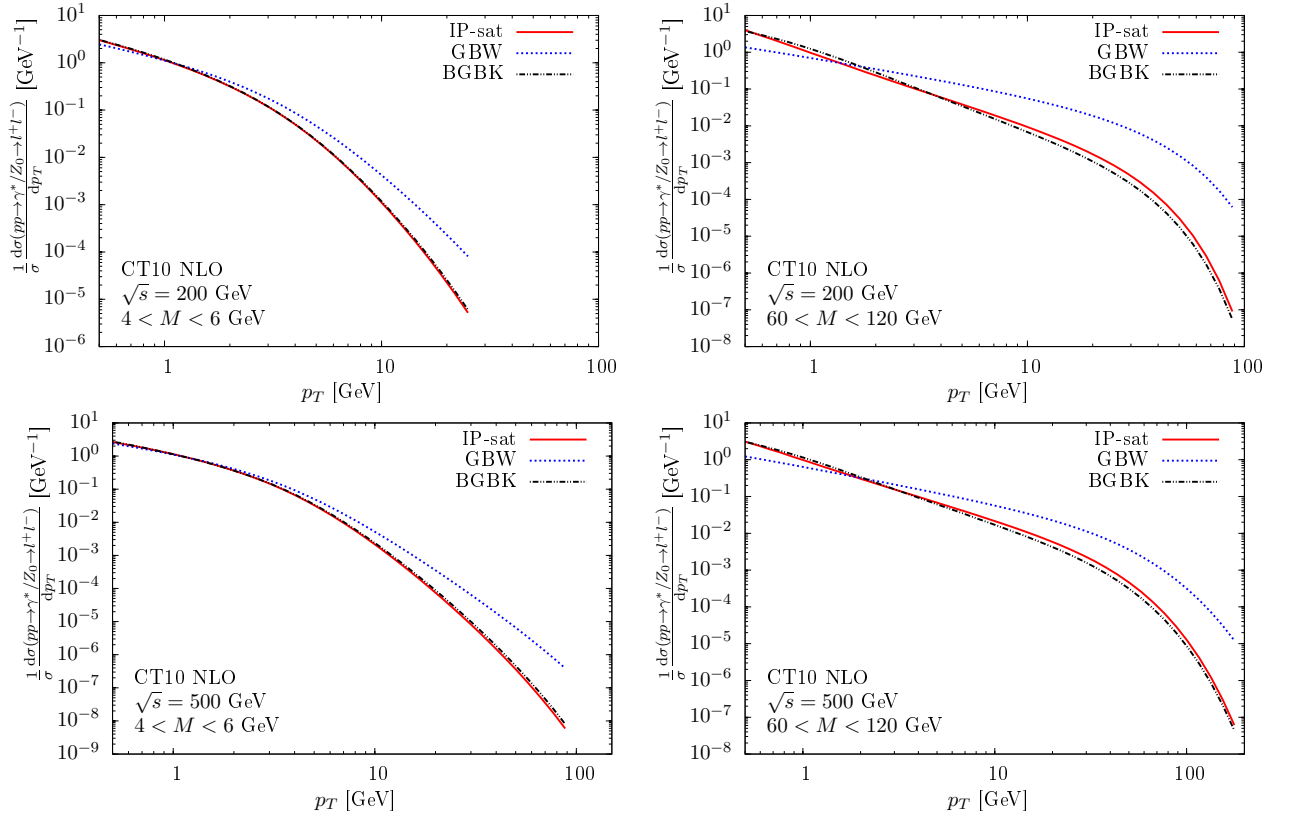


FIG. 7: The transverse momentum distributions for DY production in pp collisions at RHIC ($\sqrt{s} = 200, 500$ TeV) considering two different invariant mass ranges.

present the corresponding distributions at RHIC energies considering two different ranges of invariant masses. At low invariant masses, where the photon contribution strongly dominates, the IP-SAT and GBW models give very similar predictions. The difference between these models rises with p_T and M . At large invariant masses probing the Z^0 peak region, the predictions differ even more significantly, and such a tendency continues to higher M . In this kinematical range, the DGLAP evolution makes the predictions more reliable at both low (RHIC) and high (LHC) energies.

B. Predictions for the azimuthal correlation function in pp collisions

Finally, let us consider the correlation function $C(\Delta\phi)$ defined by Eq. (17). This observable has been studied in Ref. [28] for the DY+pion production in proton(deuteron)-nucleus collisions at RHIC and LHC energies taking into account saturation effects and considering only the virtual photon contribution to dilepton production, $\gamma^* \rightarrow l\bar{l}$. The authors have demonstrated that at variance to the near-side peak ($\Delta\phi = 0$) distribution, which is dominated by the leading jet fragmentation, the away-side peak ($\Delta\phi = \pi$) follows from back-to-back jets produced in the hard $2 \rightarrow 2$ scattering. Moreover, since low- x gluons in the target dominate and carry a typically large transverse momentum of the order of the saturation scale, the transverse momentum imbalance of back-to-back jets increases at high energies. So saturated gluons from the target tend to smear the back-to-back structure and suppress the away-side peak in the $\Delta\phi$ distribution.

There are two main important results coming from the analysis in Ref. [28]. The first one is the prediction of a double peak in the correlation function distribution around $\Delta\phi = \pi$ with a dip at $\Delta\phi = \pi$. The second shows that such a behaviour of $C(\Delta\phi)$ is not strongly dependent on the large transverse momentum tail of the UGDF, which was used in calculations. The latter conclusion implies that it is possible to get realistic predictions employing also the GBW model for the dipole cross section. In this case, numerical calculations are significantly simplified and the

UGDF has the following analytical form,

$$F(x_g, k_T^g) = \frac{1}{\pi Q_s^2(x_g)} e^{-k_T^{g,2}/Q_s^2(x_g)}, \quad (28)$$

with the saturation scale given by Eq. (23). In what follows, we study the correlation function $C(\Delta\phi)$ assuming the GBW model for the UGDF, the CT10 NLO parametrization for parton distributions and the Kniehl-Kramer-Potter (KKP) fragmentation function $D_{h/f}(z_h, \mu_F^2)$ of a quark with a flavor f into a neutral pion $h = \pi^0$ [63]. Moreover, we assume that a minimal transverse momentum (p_T^{cut}) for the gauge boson G and pion in Eq. (17) is the same and is equaled to 1.5 and 3.0 GeV for RHIC and LHC energies, respectively.

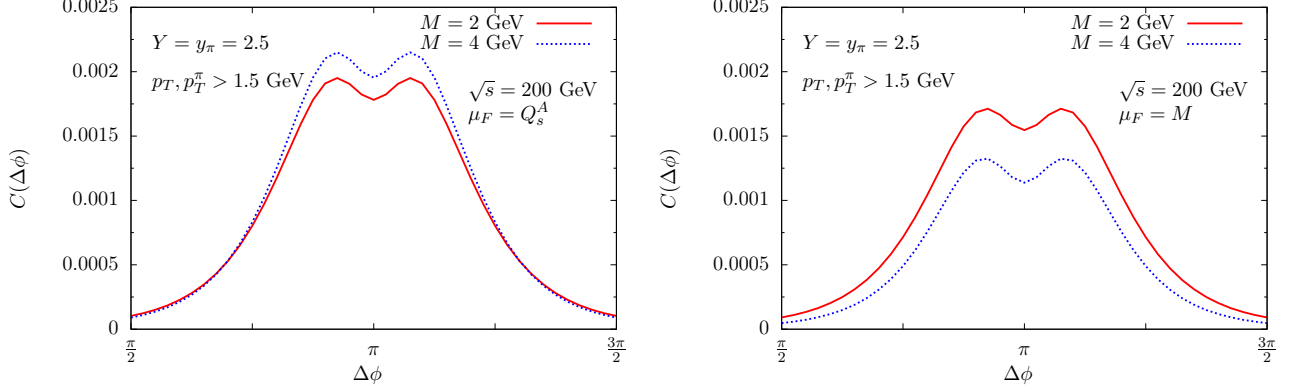


FIG. 8: The correlation function $C(\Delta\phi)$ for the associated DY pair and pion production in dAu collisions at RHIC ($\sqrt{s} = 200$ GeV) assuming that factorization scale is given by the nuclear saturation scale $\mu_F = Q_s^A$ (left panel) or by the dilepton invariant mass $\mu_F = M$ (right panel).

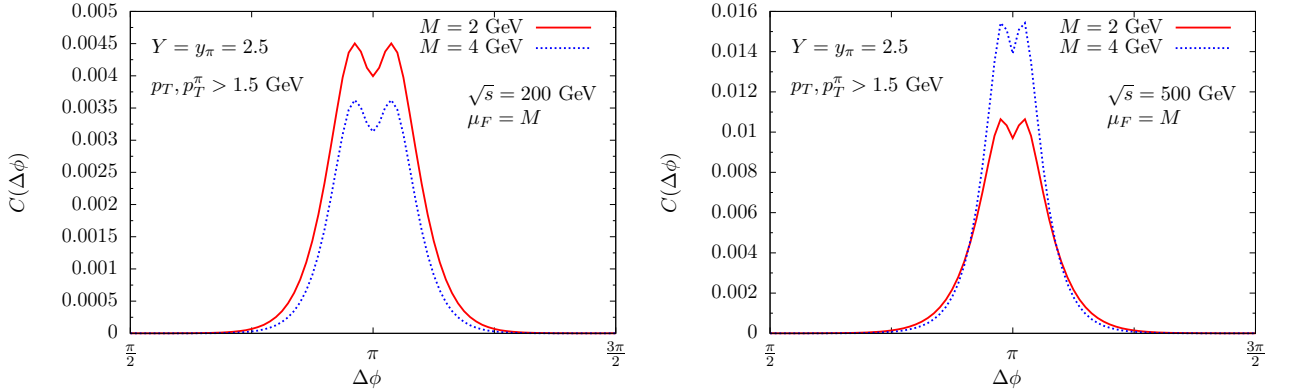


FIG. 9: The correlation function $C(\Delta\phi)$ for the associated DY pair and pion production in pp collisions at RHIC ($\sqrt{s} = 200, 500$ GeV).

At first, we test our calculations comparing our results with those presented in Ref. [28] for dAu collisions at RHIC ($\sqrt{s} = 200$ GeV). For this reason, following Ref. [28] we take the same saturation scale $Q_{s,A}$ for a target nucleus with the mass number A defined in terms of the corresponding scale $Q_s(x)$ for the proton target in the GBW parametrisation, $Q_{s,A}^2(x) = A^{1/3} c(b) Q_s^2(x)$, where $c = c(b)$ is the profile function as a function of impact parameter b (for central collisions we used $c = 0.85$ and assume a naive GBW profile of the dipole-nucleus cross section following Ref. [28]). Our results for forward particles $Y = y_\pi = 2.5$ and two different values of the dilepton invariant mass M are presented in the left panel of Fig. 8 adopting that the factorization scale of the considered process is determined by the nuclear saturation scale, i.e. $\mu_F = Q_s^A$. Similarly as is in Ref. [28] we obtain the double-peak structure of $C(\Delta\phi)$ in the away-side dilepton-pion angular correlation with the magnitude of peaks increasing with the dilepton invariant mass and the width of the double peak increasing with the saturation scale. The normalisation of the curves

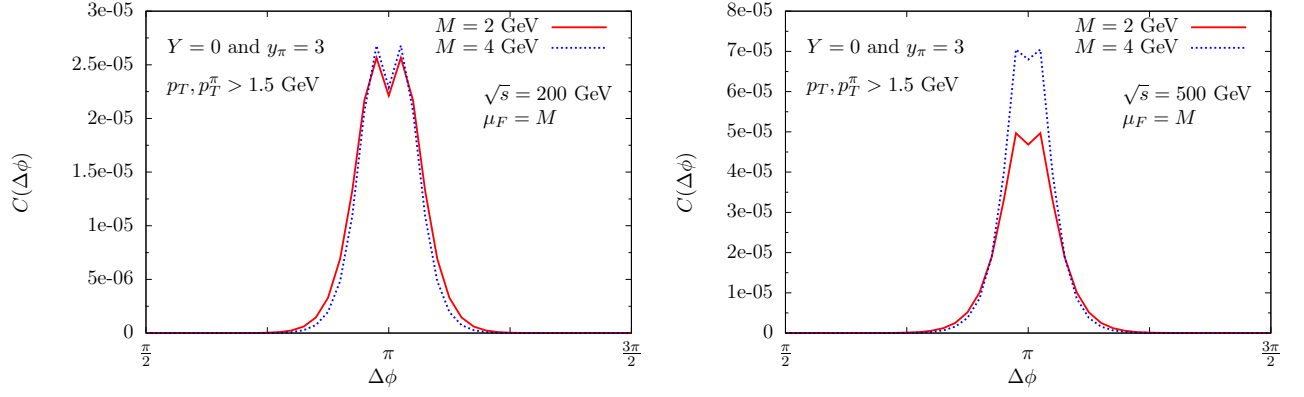


FIG. 10: The correlation function $C(\Delta\phi)$ for the the associated DY pair and pion production in pp collisions at RHIC ($\sqrt{s} = 200, 500$ GeV) for different values of the photon and pion rapidities.

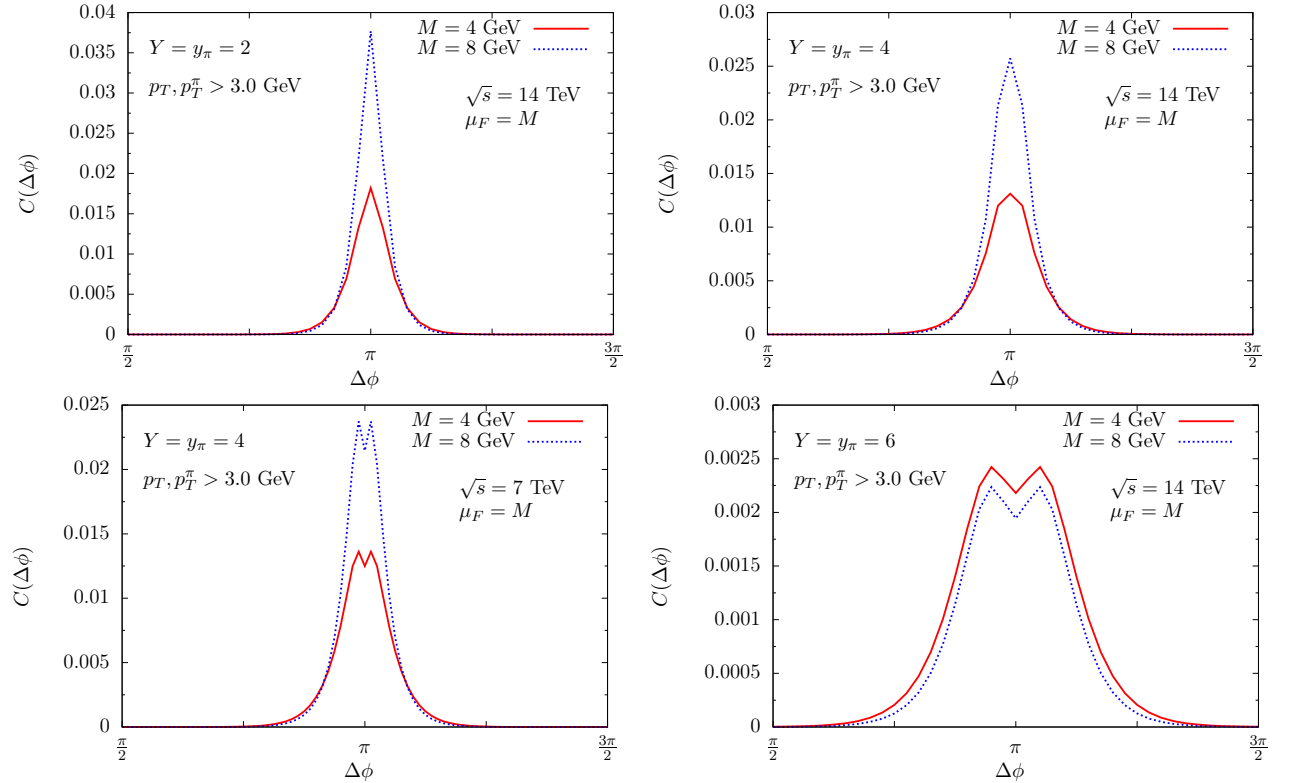


FIG. 11: The correlation function $C(\Delta\phi)$ for the associated DY pair and pion production in pp collisions at LHC ($\sqrt{s} = 7, 14$ TeV) for several values of the gauge boson and pion rapidities.

turns out to be slightly different from that in Ref. [28] due to different sets of parton distributions and fragmentation functions used in our calculations, but an overall agreement is rather good.

As the leading order, from the instructive point of view we test an arbitrary choice of the factorization scale analyzing the impact of different scale choice on results of calculation of $C(\Delta\Phi)$. Therefore, in the right panel of Fig. 8 we present prediction for the dilepton-pion correlation function in dAu collisions at RHIC for the factorization scale $\mu_F = M$. Such a choice of the factorization scale is motivated by the fact that we would like to extend the formalism used in Ref. [28] also for pp collisions and kinematical range of large invariant masses where $Z^0 \rightarrow l\bar{l}$ should be included. Fig. 8 clearly demonstrates that predicted double-peak structure of the correlation function in dAu collisions is not affected by a choice of the factorization scale. Consequently, the same result is expected also for pp

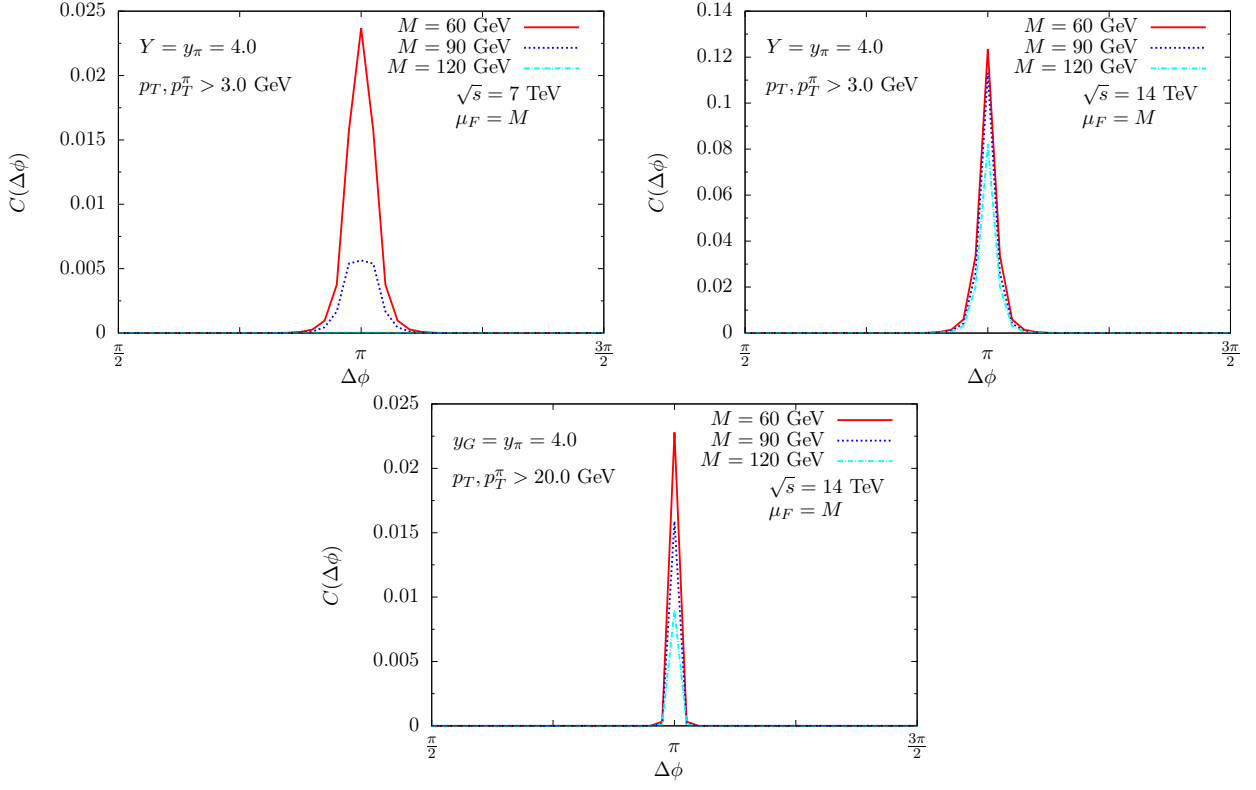


FIG. 12: The correlation function $C(\Delta\phi)$ for the the associated DY pair and pion production in pp collisions at two different LHC collision energies, $\sqrt{s} = 7$ and 14 TeV and two different values of the minimum cut-off $p_T^{\text{cut}} = 3$ and 20 GeV on the gauge boson and pion transverse momenta.

collisions as will be shown below.

Now let us switch on to investigation of the correlation function in pp collisions. Figs. 9 and 11 show our predictions for the correlation function in the range of low invariant masses dominated by the virtual photon channel, $\gamma^* \rightarrow l\bar{l}$. In particular, Figs. 9 and 11 demonstrate that the double peak structure emerges in pp collisions at both RHIC and LHC energies considering that the photon and pion are produced at forward rapidities, close to the phase space limit. The double peak structure of $C(\Delta\phi)$ is also predicted at RHIC energies for different values of the photon (central) and pion (forward) rapidities with corresponding results shown in Fig. 10. It is important to emphasize that such forward-central correlations can be experimentally studied by the STAR Collaboration in both pp and pA collisions. In Fig. 11 we present the correlation function in pp collisions at $\sqrt{s} = 14$ TeV considering different values of the dilepton pair and pion rapidities. We predict that the double-peak structure of $C(\Delta\phi)$ arises only for pions at large forward rapidities, where the saturation scale takes values of the order of the dilepton invariant mass. Indeed, at large pion rapidities the saturation scale increases and becomes non-negligible compared to the typical transverse momentum of the back-to-back particles which induces a noticeable decorrelation between them. Consequently, results in Fig. 11 also demonstrate that the study of the rapidity dependence of the correlation function in pp collisions at the LHC Run II can be useful to probe the onset of saturation effects.

Finally, in Fig. 12 we present our predictions for $C(\Delta\phi)$ at large values of the dilepton invariant mass imposed by the virtual $Z^0 \rightarrow l\bar{l}$ channel and Z^0/γ interference. In the top left and top right panels we present our results at c.m. energy $\sqrt{s} = 7$ and 14 TeV, respectively, assuming that $p_T^{\text{cut}} = 3$ GeV. For comparison, in the bottom panel we also present results considering larger $p_T^{\text{cut}} = 20$ GeV. In all cases, we obtain a sharp peak for $\Delta\phi \approx \pi$, which is characteristic for the back-to-back kinematics of final states. Such a result is expected since at large invariant masses where the effect of the intrinsic transverse momentum of gluons, which is of the order of the saturation scale, is negligible.

IV. SUMMARY

In this paper, we presented an extensive phenomenological analysis of the inclusive DY process $pp \rightarrow (\gamma^*/Z^0 \rightarrow l\bar{l})X$ within the color dipole approach. At large dilepton invariant masses the Z^0 contribution to DY process becomes relevant. The corresponding predictions for the integrated Z^0 boson production cross section as well as the dilepton invariant mass, rapidity and transverse momentum differential distributions have been compared with available data at different c.m. energies from Tevatron to LHC. The results were obtained employing recent IP-SAT and BGBK parametrisations for the dipole cross section accounting for the DGLAP evolution of the gluon density in the target nucleon. This allowed to improve an agreement with the data mainly at large invariant mass ranges.

Besides, we have studied correlation function $C(\Delta\phi)$ in azimuthal angle between the produced dilepton and a pion, which results from a fragmentation of a projectile quark radiating the virtual gauge boson. The corresponding predictions has been performed at various c.m. energies for both low and high dilepton invariant mass ranges as well as at different rapidities of final states. We found a characteristic double-peak structure of the correlation function around $\Delta\phi \simeq \pi$ in the case of low dilepton mass, $M \sim Q_s$ and for pion production at large forward rapidities. Moreover, Figs. 8 and 9 clearly demonstrate that the width of a double peak around $\Delta\phi \simeq \pi$ is strongly correlated with the magnitude of the saturation scale Q_s . For this reason, a detailed investigation of the correlation function by the future measurements at RHIC and LHC allows to set stronger constraints on the UGDF models and hence to dipole model parametrisations offering thus a possibility for more direct measurements of the saturation scale.

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